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Introduction

The Xilinx® LogiCORE™ IP Discrete Fourier Transform (DFT) core meets the requirements for 3GPP Long Term Evolution (LTE) [Ref 1] systems.

The point size of the transformation (N) can be specified on a frame-by-frame basis and can take the values $N=2^M \times 3^P \times 5^Q$, where M, P, and Q can be set to a range of values (as in Table 3-1) that meet the LTE system requirements.

Features

- Support for wide range of transform sizes, including 1296 and 1536
- Less than 26 μs total latency when transforming 1200 points at 245.76 MHz (using any combination of sizes)
- Size can be changed for each transform
- Up to 18-bit twos complement input data width, up to 18-bit twos complement output data width with 4-bit block exponent
- Direct and inverse DFT supported on frame-by-frame basis

<table>
<thead>
<tr>
<th>LogiCORE IP Facts Table</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Core Specifics</strong></td>
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<tr>
<td>Supported Device Family(1)</td>
</tr>
<tr>
<td></td>
</tr>
<tr>
<td></td>
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<tr>
<td></td>
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<td>Supported User Interfaces</td>
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<td>Design Files</td>
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<td>Test Bench</td>
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<td></td>
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<td>Synthesis</td>
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<tr>
<td><strong>Support</strong></td>
</tr>
<tr>
<td>Provided by Xilinx at the Xilinx Support web page</td>
</tr>
</tbody>
</table>

Notes:
1. For a complete listing of supported devices, see the Vivado IP catalog.
2. For the supported versions of the tools, see the Xilinx Design Tools: Release Notes Guide.
Overview

The Discrete Fourier Transform IP core implements forward and inverse DFTs for a wide range of user-selectable point sizes. The point size and transform direction may be changed on a per-frame basis. The core supports input data widths of 8 to 18 bits, in two's complement format.

Feature Summary

The Discrete Fourier Transform core supports a wide range of point sizes, including 1296 and 1536 for the 3GPP LTE standard. The point size and the transform direction may be changed on a frame-by-frame basis.

A bit-accurate C model is delivered with the core to support software simulation.

Applications

The Discrete Fourier Transform core may be used to perform a forward or inverse Fourier transform on data frames which are not a power of two in size.

The supported point sizes cover the requirements of the 3GPP LTE standard for a DFT in the baseband uplink. The core may also be used for general DFT applications such as spectral analysis or convolution in the frequency domain.

Licensing and Ordering Information

This Xilinx® LogiCORE™ IP module is provided at no additional cost with the Xilinx Vivado® Design Suite under the terms of the Xilinx End User License. Information about this and other Xilinx LogiCORE IP modules is available at the Xilinx Intellectual Property page. For information about pricing and availability of other Xilinx LogiCORE IP modules and tools, contact your local Xilinx sales representative.
Chapter 2

Product Specification

The forward DFT output is related to the input by the following equation:

\[ X(k) = \sum_{n=0}^{N-1} x(n)e^{\frac{-j2\pi nk}{N}} \quad k = 0, \ldots, N-1 \]

where \( j = \sqrt{-1} \) and the input, \( x(n) \), is a complex quantity \( x_r(n) + jx_i(n) \) in which \( x_r(n) \) and \( x_i(n) \) are two's complement fixed-point numbers whose values are given by:

\[ x = -x_{17} + \sum_{t=0}^{16} x_t2^{-17+t} \]

where \( x_t \) is the \( t \)-th bit of \( x \).

The output \( X(k) \) is a complex block floating-point quantity whose value is given by:

\[ (X_r(k) + jX_i(k))2^b \]

where \( X_r(k) \) and \( X_i(k) \) are two's complement numbers as defined previously, and the block exponent, \( b \), is an unsigned integer with weighted binary representation:

\[ b = \sum_{t=0}^{3} b_t2^t \]

where \( b_t \) is the \( t \)-th bit of \( b \). The block exponent is constant for all elements of a particular DFT output frame.

The inverse DFT has the following relationship between input and output:

\[ x(n) = \sum_{k=0}^{N-1} X(k)e^{\frac{j2\pi nk}{N}} \quad n = 0, \ldots, N-1 \]
Again, the input is represented as a complex two's complement fixed-point value, and the output a complex block floating-point value, as defined for the forward transform.

Note that neither the forward nor inverse DFT provides scaling by 1/N.

**Format of Input/Output Data**

For all bit widths, the fixed point is to the right of the MSB, that is, such that data ‘x’ takes the range \(-1.0 \leq x < 1.0\). For best numerical performance two's complement input data, that is, less than 18-bits should be zero padded in the least significant bit positions.

Block exponent (BLK_EXP) is the power of 2 in the block floating point representation for the output data. Its range is from 0 to 15.

---

**Performance**

**DFT Throughput**

The throughput of the design, measured in terms of the number of DFTs per cycle, is given by \(1/C_T\) where \(C_T\) is the total number of cycles between frames of input data. The value of \(C_T\) for each transform size is summarized in Table 3-1.

**DFT Latency**

**Single Transform Latency**

The minimum latency of the core is defined as the number of cycles from first input to last output. It is summarized in Table 3-1.

**Multiple Transform Latency**

The minimum latency for multiple transforms is obtained by adding the values of \(C_T\) for each size, and \(C_L\) for the last transform. The latency for \(V\) transforms of the same size is given by the following equation:

\[
\text{Total Latency} = (V-1)C_T + C_L
\]

The time to process 1200 points, as summarized in Table 3-1 and Table 3-2, has been derived from the preceding equation and the clock period. Note that for point sizes larger than 600, \(V\) is given by 1200/N, where N is the point size. The choice of 1200 point as the size is driven by the fact that 1200 point array seems to be the most typical case in the LTE systems.
Resource Utilization

For full details about performance and resource utilization, visit the Performance and Resource Utilization web page.

Port Descriptions

The pin-out of the DFT is summarized in Table 2-1.

Table 2-1: Pinout

<table>
<thead>
<tr>
<th>Name</th>
<th>Width</th>
<th>Direction</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>XN_RE</td>
<td>N(1)</td>
<td>INPUT</td>
<td><strong>Real Data Input</strong>: Provide in twos complement fixed-point format. Provide in natural order.</td>
</tr>
<tr>
<td>XN_IM</td>
<td>N(1)</td>
<td>INPUT</td>
<td><strong>Imaginary Data Input</strong>: Provide in twos complement fixed-point format. Provide in natural order.</td>
</tr>
<tr>
<td>FD_IN</td>
<td>1</td>
<td>INPUT</td>
<td><strong>First Data In</strong>: Set High to indicate start of data input frame. FD_IN is ignored when RFFD is Low.</td>
</tr>
<tr>
<td>RFFD</td>
<td>1</td>
<td>OUTPUT</td>
<td><strong>Ready For First Data</strong>: High when the core is ready for a new frame of data. Goes Low one cycle after a valid FD_IN.</td>
</tr>
<tr>
<td>SIZE</td>
<td>6</td>
<td>INPUT</td>
<td><strong>Size In</strong>: Size of transform to be performed. Sampled when FD_IN is High (that is, at start of data frame).</td>
</tr>
<tr>
<td>FWD_INV</td>
<td>1</td>
<td>INPUT</td>
<td><strong>Transform Direction</strong>: Set High to perform forward transform or Low for inverse transform. Sampled when FD_IN is High (that is, at start of data frame).</td>
</tr>
<tr>
<td>SCLR</td>
<td>1</td>
<td>INPUT</td>
<td><strong>Synchronous Clear</strong>: Set High for a single cycle to reset the core. This must be performed after power-on. If the core is processing data at the time a reset is performed, then processing is halted immediately and any intermediate data is discarded. After reset the core is ready to accept new input frames.</td>
</tr>
<tr>
<td>CLK</td>
<td>1</td>
<td>INPUT</td>
<td>Clock</td>
</tr>
<tr>
<td>CE</td>
<td>1</td>
<td>INPUT</td>
<td><strong>Clock Enable</strong>: Clock enable has lower precedence than SCLR</td>
</tr>
<tr>
<td>XK_RE</td>
<td>N(1)</td>
<td>OUTPUT</td>
<td><strong>Real Data Output</strong>: Provided in natural order and in fixed-point format.</td>
</tr>
<tr>
<td>XK_IM</td>
<td>N(1)</td>
<td>OUTPUT</td>
<td><strong>Imaginary Data Output</strong>: Provided in natural order and in fixed-point format.</td>
</tr>
<tr>
<td>BLK_EXP</td>
<td>4</td>
<td>OUTPUT</td>
<td><strong>Block exponent</strong>: Provided as unsigned integer.</td>
</tr>
<tr>
<td>FD_OUT</td>
<td>1</td>
<td>OUTPUT</td>
<td><strong>First Data Out</strong>: Set High by core to indicate that the core is ready to output data.</td>
</tr>
<tr>
<td>DATA_VALID</td>
<td>1</td>
<td>OUTPUT</td>
<td><strong>Data Valid</strong>: Set High by core to indicate that data output is valid.</td>
</tr>
</tbody>
</table>

Notes:
1. N is number of bits per single value, real or imaginary.
Chapter 3

Designing with the Core

This chapter includes guidelines and additional information to facilitate designing with the core.

Clocking

The core requires a single clock, \( \text{CLK} \), and is active-High triggered. If selected, the active-High clock enable, \( \text{CE} \), stalls all core processing when de-asserted.

Resets

The DFT has a single active-High synchronous reset, \( \text{SCLR} \). Asserting \( \text{SCLR} \) for a single cycle resets the core. \( \text{SCLR} \) overrides \( \text{CE} \) if both controls are present on the core.

Protocol Description

The DFT design has a fully synchronous interface. Figure 3-1 shows the pinout of the design. See Table 2-1 for more details on ports.
The core indicates that it is ready to accept a new frame of data by setting RFFD High. When RFFD is High, data input may be started by setting FD_IN High for one or more cycles. Data is input via XN_RE and XN_IM. It should be provided over N cycles without interruption. Data input and output are complex and in natural order. FD_OUT signals when the core starts data output and DATA_VALID signals when data on XK_RE and XK_IM is valid.

Note that FD_IN is ignored while RFFD is Low, and so FD_IN can be kept High for multiple cycles. FD_IN is accepted on the first cycle that RFFD is High.

If FD_IN is set permanently High, then the core will start a new frame of data input as soon as the core is ready. This arrangement provides maximum transform throughput. Alternatively, RFFD may be connected directly to FD_IN to achieve the same behavior.

The first element of input data should be provided on the same cycle that the core starts to receive data, that is, the first cycle in which both FD_IN and RFFD are High.

Input and Output Timing

Figure 3-2 provides a timing diagram for the DFT input and output. It shows a forward transform being followed by an inverse transform.

Data input and output is partially overlapped with processing to minimize the latency, C_L, of the core. Initially, input data is copied into the intermediate buffer. Once 3N/4 elements have been written to the buffer, the DFT starts performing the first layer of radix-4 operations (denoted R4 in Figure 3-2). Subsequent input data is fed directly into the DFT as each radix-4 operation is performed.

Similarly, data output is overlapped with the last layer of radix-3 operations (denoted R3 in Figure 3-2), with the first N/3 samples coming directly from the radix-r unit. The remaining
outputs of the radix-r unit are temporarily stored in the intermediate buffer and output over the next 2N/3 cycles.

![Interface Timing Diagram](image)

**Figure 3-2: Interface Timing Diagram**

### Encoding of Size Parameter

The transform size, N, should be selected via the SIZE input using the binary encoding presented in Table 3-1. For each transform size, the table also indicates the latency of the design, C_L, and minimum cycles between input frames, C_T. The latency is defined here as the number of cycles between the first element of input data and last element of output data.

Also shown in Table 3-1 is the total time to operate on 1200 points using N-point transforms. For example, when N=12 this is the time to perform 100 12-point transforms.

Additional size 1536 can be selected only if the core synthesized with the “Support size 1536” parameter on. Then the core requires one extra block RAM to store the additional coefficients and will run slightly slower.

<table>
<thead>
<tr>
<th>Table 3-1: Support for DFT Transform Size</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Size (Binary)</strong></td>
</tr>
<tr>
<td>-------------------</td>
</tr>
<tr>
<td>0</td>
</tr>
<tr>
<td>1</td>
</tr>
</tbody>
</table>
### Table 3-1: Support for DFT Transform Size (Cont’d)

<table>
<thead>
<tr>
<th>Size (Binary)</th>
<th>N</th>
<th>M (Radix-2)</th>
<th>P (Radix-3)</th>
<th>Q (Radix-5)</th>
<th>Latency C&lt;sub&gt;L&lt;/sub&gt; Cycles</th>
<th>Period C&lt;sub&gt;T&lt;/sub&gt; Cycles</th>
<th>Time to Process 1200 Points, μs (at 245.76 MHz)</th>
</tr>
</thead>
<tbody>
<tr>
<td>2</td>
<td>36</td>
<td>2</td>
<td>2</td>
<td></td>
<td>152</td>
<td>139</td>
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<td>176</td>
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<td>1</td>
<td>227</td>
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<tr>
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<td>17.63&lt;sup&gt;(1)&lt;/sup&gt;</td>
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<td>9</td>
<td>1</td>
<td>0</td>
<td>4727</td>
<td>4714</td>
<td>19.24&lt;sup&gt;(1)&lt;/sup&gt;</td>
</tr>
</tbody>
</table>

**Notes:**
1. These times are given for the full transform rather than for 1200 point size.
DFT Operation

The N-point DFT is decomposed into relatively prime factors: $2^M$, $3^P$ and $5^Q$, where the total transform size is given by $N=2^M \times 3^P \times 5^Q$. This is shown diagrammatically in Figure 3-3.

![Factorization of DFT](image)

Each prime factor is implemented by breaking it down into the appropriate number of common factors. These are implemented using radix-2, -3, -4 and -5 butterfly operations as shown in Figure 3-4. Note that the $2^M$ prime factor has been implemented using a combination of radix-2 and radix-4 butterflies. The multiplications required between common factors are not shown, and are implemented within the butterfly, on its input.

![Full Factorization of DFT](image)

The radix-2, -3, -4, and -5 operations are performed using a single pipelined, parallel radix-r unit. This is capable of performing two radix-2 operations per clock cycle, one radix-3 or radix-4 operation per cycle and one radix-5 operation per two clock cycles as shown in Figure 3-5.

![Radix-r Unit](image)
**Radix-r Unit**

Figure 3-6 and Figure 3-7 show the radix-3 and radix-5 butterfly operations used by the DFT. They include the *twiddle factor* multiplications on the input required to cascade factors to obtain a $2^M \times 3^P \times 5^Q$ point DFT. The diagrams also show the internal word lengths adopted, and include the scaling and rounding blocks required to implement block-floating-point. Their function is explained in the next section.

The radix-5 butterfly is performed using two passes of the radix-r unit. The first pass performs the twiddle-factor multiplications and first two stages of adders. At this point, scaling and rounding are applied to reduce word length to that of the input, so that it may be fed back for the second pass. The worst-case word growth for the first half is equivalent to that of the whole butterfly, so no further scaling is applied in the second pass. The second pass performs the intermediate multiplies and the final two stages of addition. Quantization reduces the word length to that of the input, so that it may be stored in the intermediate memory, ready for the next stage.

**Figure 3-6: Radix-3 Winograd Butterfly**
Block Floating-Point Behavior

Word length growth within the transform is accommodated by block floating-point. This is achieved by scaling the output of the radix-\( r \) unit by a power of 2 to keep a data word length of 18-bits. To reduce implementation cost, the level of scaling is either 0, 1, 2 or 3-bit shift, allowing its implementation using a 4:1 multiplexer.

The level of scaling is calculated by establishing the maximum size of the layer input, and the maximum word growth possible through the layer.

This growth is \( \log_2(1 + (r - 1) \sqrt{2}) \) bits per radix-\( r \) layer. The \( \sqrt{2} \) scaling occurs when a complex input with full-scale positive or negative real or imaginary parts, is rotated by 45 degrees. Rotations are required between layers as a result of the factorization of the DFT algorithm. The first layer requires no twiddle-factors, and so the word growth is exactly 2 bits and the associated scaling is 1/4, which is obtained by a 2-bit right-shift. The worst-case scaling applied for each radix is summarized in Table 3-2.

Table 3-2: Power-of-2 Scaling Required to Accommodate Worst-Case Growth

<table>
<thead>
<tr>
<th>Radix-4</th>
<th>Layer</th>
<th>Worst-Case Growth</th>
<th>Power-2 Scaling</th>
</tr>
</thead>
<tbody>
<tr>
<td>Radix-2</td>
<td></td>
<td>2.414</td>
<td>4</td>
</tr>
<tr>
<td>Radix-3</td>
<td></td>
<td>3.828</td>
<td>4</td>
</tr>
<tr>
<td>Radix-4</td>
<td>First layer</td>
<td>2.000</td>
<td>2</td>
</tr>
<tr>
<td>Radix-4</td>
<td>Other layer</td>
<td>5.243</td>
<td>8</td>
</tr>
<tr>
<td>Radix-5</td>
<td></td>
<td>6.657</td>
<td>8</td>
</tr>
</tbody>
</table>
The maximum absolute value of the input is established by examining the butterfly output from the previous layer. This examination is done as the outputs are calculated and written to memory, and so the final value is the maximum across the whole layer. To minimize resources, the butterfly outputs are truncated to 4 bits before the absolute value is calculated. The maximum absolute value is used to establish a margin, in terms of bits. This margin is the number of bits by which an input might grow without overflow (that is, the number of leading zeros or ones, excluding sign in the largest term).

Table 3-3: Establishing Margin from the Maximum Absolute Value

<table>
<thead>
<tr>
<th>Maximum Absolute Value (x)</th>
<th>Margin</th>
</tr>
</thead>
<tbody>
<tr>
<td>$x \geq 0.5$</td>
<td>0</td>
</tr>
<tr>
<td>$0.25 \leq x &lt; 0.5$</td>
<td>1</td>
</tr>
<tr>
<td>$0.125 \leq x &lt; 0.25$</td>
<td>2</td>
</tr>
<tr>
<td>$x &lt; 0.125$</td>
<td>3</td>
</tr>
</tbody>
</table>

The required scaling is, therefore, the worst-case scaling reduced by the margin, with negative values being set to zero. The scaling applied at each layer is summed, and provided as the block floating-point exponent with the complex output data.
Chapter 4

Design Flow Steps

This chapter describes customizing and generating the core, constraining the core, and the simulation, synthesis and implementation steps that are specific to this IP core. More detailed information about the standard Vivado® design flows and the IP integrator can be found in the following Vivado Design Suite user guides:

- Vivado Design Suite User Guide: Designing IP Subsystems using IP Integrator (UG994) [Ref 2]
- Vivado Design Suite User Guide: Designing with IP (UG896) [Ref 3]
- Vivado Design Suite User Guide: Getting Started (UG910) [Ref 4]
- Vivado Design Suite User Guide: Logic Simulation (UG900) [Ref 5]

Customizing and Generating the Core

This section includes information about using Xilinx tools to customize and generate the core in the Vivado Design Suite.

If you are customizing and generating the core in the Vivado IP Integrator, see the Vivado Design Suite User Guide: Designing IP Subsystems using IP Integrator (UG994) [Ref 2] for detailed information. IP Integrator might auto-compute certain configuration values when validating or generating the design. To check whether the values do change, see the description of the parameter in this chapter. To view the parameter value you can run the validate_bd_design command in the Tcl console.

Vivado Integrated Design Environment

You can customize the IP for use in your design by specifying values for the various parameters associated with the IP core using the following steps:

1. Select the IP from the IP catalog.
2. Double-click the selected IP or select the Customize IP command from the toolbar or right-click menu.

For details, see the Vivado Design Suite User Guide: Designing with IP (UG896) [Ref 3] and the Vivado Design Suite User Guide: Getting Started (UG910) [Ref 4].
The DFT core GUI has a single page with fields to set parameter values for the particular instantiation required. This section provides a description of each field.

**Component Name:** The name of the core component to be instantiated. the name must begin with a letter and be composed of the following characters: a to z, 0 to 9, and "_".

**Precision Options:** Selects the input and output data width required.

**Optimization:** Selects whether the core should be optimized for resources or performance.

**Optional Pins:**
- CE: Selects if the core has a clock enable control pin.
- SCLR: selects if the core has a synchronous reset control pin.

**Enable 1536 point size support:** Enables support for the 1536-point transform for 3GPP LTE systems. Selecting this option requires additional hardware resources.

**User Parameters**

Table 4-1 shows the relationship between the GUI fields in the Vivado IDE (described in Vivado Integrated Design Environment) and the User Parameters (which can be viewed in the Tcl console).

<table>
<thead>
<tr>
<th>GUI Parameter</th>
<th>User Parameter</th>
<th>Default Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Input/Output Data Width</td>
<td>data_width</td>
<td>18</td>
</tr>
<tr>
<td>Optimization</td>
<td>speed_optimization</td>
<td>Area</td>
</tr>
<tr>
<td>CE</td>
<td>clock_enable</td>
<td>False</td>
</tr>
<tr>
<td>SCLR</td>
<td>synchronous_clear</td>
<td>True</td>
</tr>
<tr>
<td>Enable 1536 point size support</td>
<td>support_size_1536</td>
<td>false</td>
</tr>
</tbody>
</table>

**Output Generation**

For details, see the Vivado Design Suite User Guide: Designing with IP (UG896) [Ref 3].

**Constraining the Core**

This section contains information about constraining the core in the Vivado Design Suite.

**Required Constraints**

This section is not applicable for this IP core.
Device, Package, and Speed Grade Selections
This section is not applicable for this IP core.

Clock Frequencies
This section is not applicable for this IP core.

Clock Management
This section is not applicable for this IP core.

Clock Placement
This section is not applicable for this IP core.

Banking
This section is not applicable for this IP core.

Transceiver Placement
This section is not applicable for this IP core.

I/O Standard and Placement
This section is not applicable for this IP core.

Simulation
For comprehensive information about Vivado simulation components, as well as information about using supported third party tools, see the *Vivado Design Suite User Guide: Logic Simulation* (UG900) [Ref 5].

Synthesis and Implementation
For details about synthesis and implementation, see the *Vivado Design Suite User Guide: Designing with IP* (UG896) [Ref 3].
The Xilinx® LogiCORE™ IP Discrete Fourier Transform (DFT) core has a bit accurate C model designed for system modeling. An example MATLAB® MEX function for MATLAB integration is also available. The C model is produced when the core is generated in the Vivado® Design Suite.

Features

- Bit accurate to DFT core
- Available for 32-bit and 64-bit Linux platforms
- Available for 32-bit and 64-bit Windows platforms
- Supports all features of the DFT that affect numerical results
- Designed for integration into a larger system model
- Example of C++ code provided showing how to use the function
- MATLAB MEX function with an example script for Windows

Overview

The DFT bit accurate C model has an interface consisting of a set of C functions that reside in a dynamic link library (shared library). Full details of the interface are given in DFT C Model Interface and an example piece of C++ code showing how to call the model is provided.

The model is also available as a MATLAB MEX function for MATLAB integration. The model is bit accurate but not cycle-accurate, so it produces exactly the same output data as the core on a frame-by-frame basis. However, it does not model the core latency or its interface signals.
Unpacking and Model Contents

Unzipping the DFT C model ZIP file produces the files shown in Table 5-1 and Table 5-2.

<table>
<thead>
<tr>
<th>Table 5-1: C Model ZIP File Contents for Linux</th>
</tr>
</thead>
<tbody>
<tr>
<td>File</td>
</tr>
<tr>
<td>----------------------------</td>
</tr>
<tr>
<td>dft_v4_0_bitacc_cmodel.h</td>
</tr>
<tr>
<td>libIp_dft_v4_0_bitacc_cmodel.so</td>
</tr>
<tr>
<td>run_bitacc_cmodel.cpp</td>
</tr>
<tr>
<td>dft_v4_0_bitacc_mex.cpp</td>
</tr>
<tr>
<td>make_dft_v4_0_mex.m</td>
</tr>
<tr>
<td>run_dft_v4_0_mex.m</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Table 5-2: C Model ZIP File Contents for Windows</th>
</tr>
</thead>
<tbody>
<tr>
<td>File</td>
</tr>
<tr>
<td>----------------------------</td>
</tr>
<tr>
<td>dft_v4_0_bitacc_cmodel.h</td>
</tr>
<tr>
<td>libIp_dft_v4_0_bitacc_cmodel.dll</td>
</tr>
<tr>
<td>libIp_dft_v4_0_bitacc_cmodel.lib</td>
</tr>
<tr>
<td>run_bitacc_cmodel.cpp</td>
</tr>
<tr>
<td>dft_v4_0_bitacc_mex.cpp</td>
</tr>
<tr>
<td>make_dft_v4_0_mex.m</td>
</tr>
<tr>
<td>run_dft_v4_0_mex.m</td>
</tr>
</tbody>
</table>

Installation

On Linux, ensure that the directory in which the file libIp_dft_v4_0_bitacc_cmodel.so is located is on your $LD_LIBRARY_PATH environment variable.

On Windows, ensure that the directory in which the file libIp_dft_v4_0_bitacc_cmodel.dll is located is either on your $PATH environment variable, or is the directory in which you run your executable that calls the DFT C model.

DFT C Model Interface

**Note:** An example C++ file, run_bitacc_cmodel.c is included that demonstrates how to call the DFT C model. See this file for examples of using the interface described in this chapter.

The C model is used through three functions declared in the header file, dft_v4_0_bitacc_cmodel.h:
struct xilinx_ip_dft_v4_0_state* 
xilinx_ip_dft_v4_0_create_state 
( 
  struct xilinx_ip_dft_v4_0_generics generics 
); 

int xilinx_ip_dft_v4_0_bitacc_simulate 
( 
  struct xilinx_ip_dft_v4_0_state* state, 
  struct xilinx_ip_dft_v4_0_inputs inputs, 
  struct xilinx_ip_dft_v4_0_outputs* outputs 
); 

void xilinx_ip_dft_v4_0_destroy_state 
( 
  struct xilinx_ip_dft_v4_0_state* state 
); 

1. To use the model, first create a state structure using the first function, 
   xilinx_ip_dft_v4_0_create_state. 

2. Then run the model using the second function, 
   xilinx_ip_dft_v4_0_bitacc_simulate, passing the state structure, an inputs 
   structure, and an outputs structure to the function. 

3. Finally, free up memory allocated for the state structure using the third function, 
   xilinx_ip_dft_v4_0_destroy_state. Each of these functions is described fully 
   below.

Create a State Structure

The first function, xilinx_ip_dft_v4_0_create_state, creates a new state structure 
for the DFT C model, allocating memory to store the state as required, and returns a pointer 
to that state structure. The state structure contains all the information required to define 
the DFT being modelled. The function is called with a structure containing the core's 
generics. The generics are all of the parameters that define the bit accurate numerical 
performance of the core. In the current version, the user should set up only one field in 
xilinx_ip_dft_v4_0_generics: C_DATA_WIDTH. It specifies the input/output and 
internal precision of the data in bits; the permitted range of C_DATA_WIDTH is 8 to 18 and 
its default value is 18. The xilinx_ip_dft_v4_0_create_state function fails with an 
error message and returns a NULL pointer if a generic is invalid.

Simulate the DFT Core

After a state structure has been created, it can be used as many times as required to 
simulate the DFT core. A simulation is run using the second function, 
xilinx_ip_dft_v4_0_bitacc_simulate. Call this function with the pointer to the 
existing state structure and structures that hold the inputs and outputs of the C model. The 
inputs structure members are shown in Table 5-3.
Chapter 5: C Model

The outputs structure, a pointer to which is passed to the `xilinx_ip_dft_v4_0_bitacc_simulate` function, has the members shown in Table 5-4.

### Table 5-4: Members of the Outputs Structure

<table>
<thead>
<tr>
<th>Member</th>
<th>Type</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>xk_re</td>
<td>int*</td>
<td>Pointer to array of integers (fixed-point representation), real part of output data.</td>
</tr>
<tr>
<td>xk_im</td>
<td>int*</td>
<td>Pointer to array of integers (fixed-point representation), imaginary part of output data.</td>
</tr>
<tr>
<td>blk_exp</td>
<td>int</td>
<td>Block exponent.</td>
</tr>
</tbody>
</table>

Notes:

1. Ensure that you allocate memory for the outputs structure and for arrays in the outputs structure.
2. Arrays `xk_re` and `xk_im` must have at least the number of elements defined by size input.
3. Arrays `xk_re` and `xk_im` use integers to represent fixed point numbers. The precision is defined by the `C_DATA_WIDTH` generic. For example, if `C_DATA_WIDTH` is 18, the 18 least significant bits of integers in `xk_re` and `xk_im` represent the 18-bit fixed point numbers that form the outputs of the DFT. Other bits are ignored.

If the `xilinx_ip_dft_v4_0_bitacc_simulate` function returns integer value 0 (zero), it completed successfully, and the outputs of the model are in the outputs structure. The table 3-3 gives complete list of the error codes returned by the function.
Destroy the State Structure

Finally, the state structure must be destroyed to free up memory used to store the state, using the third function, `xilinx_ip_dft_v4_0_destroy_state`, called with the pointer to the existing state structure.

If the generics of the core need to be changed, destroy the existing state structure and create a new state structure using the new generics.

### Compiling with the DFT C Model

Place the header file, `dft_v4_0_bitacc_cmodel.h`, with your other header files. Compilation varies from platform to platform.

#### Linux (32-bit and 64-bit)

Reference the shared library file used by the model, `libIp_dft_v4_0_bitacc_cmodel.so`.

Using GCC, linking is typically achieved by adding the following command line options:

```
-L. -lIp_dft_v4_0_bitacc_cmodel
```

**Note:** This assumes that the shared object libraries are in the current directory. If this is not the case, the `-L` option should be changed to specify the library search path to use.

On Linux, ensure that the directory in which the file, `libIp_dft_v4_0_bitacc_cmodel.so` is located is on your `$LD_LIBRARY_PATH` environment variable.

Here is an example GCC command line:

```
gcc -x c++ run_bitacc_cmodel.cpp -o run_bitacc_cmodel -L. -lIp_dft_v4_0_bitacc_cmodel
```

The specific syntax can differ depending on the user settings, and because the library was compiled with GNU C++ compiler v4.1.1, the compiler has to be compatible with it.

---

<table>
<thead>
<tr>
<th>Return Value</th>
<th>Error</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>No error</td>
</tr>
<tr>
<td>1</td>
<td>Undefined input data structure</td>
</tr>
<tr>
<td>2</td>
<td>Undefined state data structure</td>
</tr>
<tr>
<td>3</td>
<td>Undefined output data structure</td>
</tr>
<tr>
<td>4</td>
<td>Data width out of range</td>
</tr>
<tr>
<td>5</td>
<td>Point size out of range</td>
</tr>
</tbody>
</table>
Windows (32-bit and 64-bit)

Under Windows you must include dft_v4_0_bitacc_cmodel.h at compile time, link against libIp_dft_v4_0_bitacc_cmodel.lib and run against the dynamic link library libIp_dft_v4_0_bitacc_cmodel.dll.

For example, for Microsoft Visual Studio, ensure that the:

- Include file, dft_v4_0_bitacc_cmodel.h, is specified in Project Properties, under Configuration Properties -> C/C++ -> Preprocessor -> General.
- Link library, libIp_dft_v4_0_bitacc_cmodel.lib, is specified under Configuration Properties -> Linker -> Input -> Additional Dependencies. Also, under Configuration Properties -> Linker -> General -> Additional Library Directories specify the location of libIp_dft_v4_0_bitacc_cmodel.lib.
- The location of the dynamic link library, libIp_dft_v4_0_bitacc_cmodel.dll, is on your path or in your working directory. If the latter, the working directory can be specified under Configuration Properties > Debugging > Working Directory.

DFT MATLAB MEX Function

To use DFT C model under MATLAB®, a MEX file has to be generated. A MATLAB script to build the MEX wrapper is provided:

```
make_dft_v4_0_mex.m
```

This script compiles a C++ MEX function using dft_v4_0_mex.cpp into a MEX file that can be used for simulation. An example script is provided to call the MEX function:

```
run_dft_v4_0_mex.m
```

The function call from MATLAB for the model is:

```
[result_array,block_exponent]= ...
    dft_v4_0_bitacc_mex(input_array, n2, n3, n5, fwdinv, precision)
```

The last two parameters can be omitted and then the default values is used (0 for fwdinv and 18 bit for precision). The input and result arrays are complex double precision arrays and block_exponent is an integer.
Appendix A

Migrating and Upgrading

This appendix contains information about migrating a design from the ISE® Design Suite to the Vivado® Design Suite, and for upgrading to a more recent version of the IP core. For customers upgrading in the Vivado Design Suite, important details (where applicable) about any port changes and other impact to user logic are included.

Migrating to the Vivado Design Suite

For information about migrating to the Vivado Design Suite, see the ISE to Vivado Design Suite Migration Guide (UG911) [Ref 6].

The Vivado IP upgrade functionality can be used to upgrade an existing XCO/XCI file from v3.0 or v3.1 to Discrete Fourier Transform v4.0. There are no changes of functionality, port or configuration from v3.1 to v4.0.

Upgrading in the Vivado Design Suite

This section provides information about any changes to the user logic or port designations that take place when you upgrade to a more current version of this IP core in the Vivado Design Suite.

Parameter Changes

No change.

Port Changes

No change.

Other Changes

No change.
Debugging

This appendix includes details about resources available on the Xilinx Support website and debugging tools.

Finding Help on Xilinx.com

To help in the design and debug process when using the Discrete Fourier Transform, the Xilinx Support web page contains key resources such as product documentation, release notes, answer records, information about known issues, and links for obtaining further product support.

Documentation

This product guide is the main document associated with the Discrete Fourier Transform. This guide, along with documentation related to all products that aid in the design process, can be found on the Xilinx Support web page or by using the Xilinx Documentation Navigator.

Download the Xilinx® Documentation Navigator from the Downloads page. For more information about this tool and the features available, open the online help after installation.

Answer Records

Answer Records include information about commonly encountered problems, helpful information on how to resolve these problems, and any known issues with a Xilinx product. Answer Records are created and maintained daily ensuring that users have access to the most accurate information available.

Answer Records for this core can be located by using the Search Support box on the main Xilinx support web page. To maximize your search results, use proper keywords such as

- Product name
- Tool message(s)
- Summary of the issue encountered
A filter search is available after results are returned to further target the results.

**Master Answer Record for the Discrete Fourier Transform**

AR: 54475

**Technical Support**

Xilinx provides technical support in the Xilinx Support web page for this LogiCORE™ IP product when used as described in the product documentation. Xilinx cannot guarantee timing, functionality, or support if you do any of the following:

- Implement the solution in devices that are not defined in the documentation.
- Customize the solution beyond that allowed in the product documentation.
- Change any section of the design labeled DO NOT MODIFY.

To contact Xilinx Technical Support, navigate to the Xilinx Support web page.

---

**Debug Tools**

There are tools available to address Discrete Fourier Transform design issues. It is important to know which tools are useful for debugging various situations.

**Vivado Design Suite Debug Feature**

The Vivado® Design Suite debug feature inserts logic analyzer and virtual I/O cores directly into your design. The debug feature also allows you to set trigger conditions to capture application and integrated block port signals in hardware. Captured signals can then be analyzed. This feature in the Vivado IDE is used for logic debugging and validation of a design running in Xilinx devices.

The Vivado logic analyzer is used with the logic debug IP cores, including:

- ILA 2.0 (and later versions)
- VIO 2.0 (and later versions)

See the Vivado Design Suite User Guide: Programming and Debugging (UG908) [Ref 7].

**C Model Reference**

See Chapter 5, C Model in this guide for tips and instructions for using the provided C Model files to debug your design.
Simulation Debug

The simulation debug flow for Mentor Graphics Questa Simulator (QuestaSim) is illustrated in Figure B-1. A similar approach can be used with other simulators.

Although versions of simulators more recent than the Vivado release might be compatible, no guarantee can be given.

The core test bench should allow the user to quickly determine if the simulator is set up correctly.

If problem is more design specific, open a case with Xilinx Technical Support and include a .wil file dump of the simulation. For the best results, dump the entire design hierarchy.

**Figure B-1: QuestaSim Debug Flow Chart**
Appendix C

Additional Resources and Legal Notices

Xilinx Resources

For support resources such as Answers, Documentation, Downloads, and Forums, see Xilinx Support.

References

These documents provide supplemental material useful with this product guide:

6. ISE® to Vivado Design Suite Migration Guide (UG911)
Revision History

The following table shows the revision history for this document.

<table>
<thead>
<tr>
<th>Date</th>
<th>Version</th>
<th>Revision</th>
</tr>
</thead>
<tbody>
<tr>
<td>11/18/2015</td>
<td>4.0</td>
<td>UltraScale+ device support added.</td>
</tr>
<tr>
<td>04/02/2014</td>
<td>4.0</td>
<td>• Added link to resource utilization figures.</td>
</tr>
<tr>
<td></td>
<td></td>
<td>• Added User Parameter table (Table 4-1).</td>
</tr>
<tr>
<td>12/18/2013</td>
<td>4.0</td>
<td>• Revision number advanced to 4.0 to align with core version number.</td>
</tr>
<tr>
<td></td>
<td></td>
<td>• Added UltraScale™ architecture support.</td>
</tr>
<tr>
<td></td>
<td></td>
<td>• Template updated.</td>
</tr>
<tr>
<td>03/20/2013</td>
<td>1.0</td>
<td>Initial release as a Product Guide; replaces DS615 and UG484. No other documentation changes.</td>
</tr>
</tbody>
</table>

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